

Cobalt (III) Oxyhydroxide as a Pyrrole Polymerization Initiator: a Theoretical Study

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Abstract: In this work, the possibility of using cobalt (III) oxyhydroxide as an electropolymerization initiator for pyrrole is studied by theoretical means. A hybrid material may be yielded by this synthesis. The mathematical model has been developed and analyzed using linear stability theory and bifurcation analysis: the steady-state stability requisites, correspondent to the synthesis efficiency, were obtained. The general causes for oscillatory and monotonic instabilities have also been detected.

Keywords: hybrid materials; polypyrrole; cobalt(III)oxyhydroxide; electrosynthesis; stable steady-state.

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1. Introduction

The conducting polymers (CP) or, better saying, intrinsically conducting polymers compose one of the most studied classes of materials in the XXI century [1–10], due to their capacity of combining the properties of plastics with metal conductivity and facility in modification. It gives them vast and rich use in:

- corrosion protecting coatings;
- capacitors and supercapacitors;
- matrices and nanoparticle stabilizers (including the matrices for hybrid materials);
- electrode modifiers in sensors and biosensors (in which the polymer coatings may play the role of active substances and(or) mediators).

The conducting polymers may be obtained either chemically or electrochemically [11–15]. Among the electrode modifying materials for assisted electropolymerization, cobalt (III) oxyhydroxide may be used. Some researchers see it as a semiconducting material as a substitute for titanium dioxide [16–20] in optical and electrochemical apparel. Its electrocatalytical and

electroanalytical activities have already been experimentally observed [19, 20] and theoretically predicted [21–23].

Nevertheless, the development of new electrosynthetic processes, especially with the indirectly induced electrooxidation includes the resolution of problems like:

- Doubts in the reaction mechanism suggestions and concerning the role of the substances taking part in the process;
- The possibility of the electrochemical instabilities, characteristic either for cobalt(III) oxyhydroxide electro-synthesis [24, 25] or for direct electropolymerization process [26–32].

Both problems may not be resolved without developing a mathematical model capable of describing the processes adequately in this system.

Therefore, the general aim of this work is the mechanistic evaluation of the possibility of pyrrole electropolymerization, assisted by CoO(OH), with the formation of their composite. It requires the satisfaction of specific objectives like:

- Suggest the reaction mechanism, including the participation of cobalt (III) oxyhydroxide in the chain initiation;
- Develop the mathematical model for this mechanism;
- Analyze the steady-state stability requirements and oscillatory and monotonic instabilities conditions using the analysis of this model;
- Compare the behavior of this system with that of analogous ones [33–35].

2. Materials and Methods

2.1. System and its Modeling.

The electropolymerization of a heterocyclic conjugated monomer may be assisted by CoO(OH) as an oxidant. In this case, for pyrrole, the reaction will be described as:



The regeneration of the oxyhydroxide is thus given as:



For the simplest case of potentiostat assisted composite electrodeposition, the process will be described by a bivariate equation set with the variables:

c – monomer concentration in the pre-surface layer;

θ – cobalt oxide anode coverage degree.

To simplify the modeling, we suppose that the reaction mixture is intensively stirred (so we may neglect the convection flow). Also, we simplify that the background electrolyte is in excess (so we can neglect the migration flow). Also, we suppose that the concentration profile of the substance is linear and its thickness to be constant, equal to δ . At its turn, cobalt (III) oxyhydroxide is supposed to cover the entire electrode surface at the beginning of the reaction.

It is possible to show that the system's behavior, in this case, will be described by a bivariate equation set as:

$$\begin{cases} \frac{dc}{dt} = \frac{2}{\delta} \left(\frac{\Delta}{\delta} (c_0 - c) - r_p \right) \\ \frac{d\theta}{dt} = \frac{1}{G} (r_p - r_o) \end{cases} \quad (1)$$

Where c_0 is the bulk monomer concentration, Δ is the diffusion coefficient, G the CoO maximal surface concentration, and r_p and r_o are electropolymerization and electrooxidation rates, described as:

$$r_p = k_p c^n (1 - \theta)^{2n-2} \quad (2)$$

$$r_o = k_o \theta \exp \frac{F\phi_0}{RT} \quad (3)$$

Where k is correspondent reaction constants, n is the number of monomer chains in the polymer, F is the Faraday number, ϕ_0 is the potential slope, related to the zero-charge potential, R is the universal gas constant, T is the absolute temperature of the solution.

This work describes the simplest case of indirect CoO(OH) -assisted electropolymerization. Its differences indirect polymerization will be described below.

3. Results and Discussion

To describe the CoO(OH) -assisted polymerization of a conjugated monomer with the example of pyrrole, we analyze the differential equation set(1) using linear stability theory. The Jacobian matrix steady-states element values may be thereby calculated as:

$$\begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix} \quad (4),$$

in which:

$$a_{11} = \frac{2}{\delta} \left(-\frac{\Lambda}{\delta} - nk_p c^{n-1} (1 - \theta)^{2n-2} \right) \quad (5)$$

$$a_{12} = \frac{2}{\delta} \left((2n - 2)nk_p c^n (1 - \theta)^{2n-3} \right) \quad (6)$$

$$a_{21} = \frac{1}{G} \left(nk_p c^{n-1} (1 - \theta)^{2n-2} \right) \quad (7)$$

$$a_{22} = \frac{1}{G} \left((2n - 2)nk_p c^n (1 - \theta)^{2n-3} - k_o \exp \frac{F\phi_0}{RT} - \xi k_o \theta \exp \frac{F\phi_0}{RT} \right) \quad (8)$$

Avoiding the cumbersome expressions during the Jacobian determinant analysis, we introduce new variables so that the determinant will be rewritten as:

$$\frac{2}{\delta G} \begin{vmatrix} -\kappa_1 - \Xi & \Omega \\ \Xi & -\Omega - \Lambda \end{vmatrix} \quad (9)$$

The general singular point conditions for the bivariate systems may be joined in Table 1.

Table 1. The main singular point conditions for the bivariate systems.

Stable steady-state	Tr $J < 0$, Det $J > 0$
Oscillatory behavior	Tr $J = 0$, Det $J > 0$
Monotonic instability	Tr $J < 0$, Det $J = 0$

It is possible to show that the oscillatory behavior in this system may be possible. Nevertheless, contrarily to the direct electropolymerization, it may be caused by a unique factor of the influences of the electrochemical process on the double electric layer capacities (DEL). The Hopf bifurcation condition may be realized only by the positivity of the parameter ξ , describing the mentioned influences. The oscillations are expected to be more frequent and have smaller amplitude than during the direct electropolymerization [29–32]. Mathematically, the condition of the oscillatory behavior may be described as (10):

$$\begin{cases} \frac{2}{\delta} (-\kappa_1 - \Xi) = \frac{1}{G} (\Lambda + \Omega) \\ \kappa_1 \Omega + \kappa_1 \Lambda + \Xi \Lambda > 0 \end{cases} \quad (10)$$

To investigate the steady-state stability, we apply the condition Tr $J < 0$, Det $J > 0$ (see the table). As shown, in the case of the relative fragility of the electrochemical stage on DEL capacitances, described by the positivity of Λ , condition (1) is warranted to be satisfied. If $\Lambda > 0$, $-\kappa_1 - \Xi - \Omega - \Lambda < 0$, due to the positivity of other parameters forming the equation. Also, $\kappa_1 \Omega + \kappa_1 \Lambda + \Xi \Lambda > 0$, if $\Lambda > 0$, also taking into account the factors mentioned above. Thus, it is possible to conclude about the electrosynthetical efficiency of this system, as the

steady-state stability is easy to obtain and maintain and, due to the absence of the side reactions, capable of compromise the electropolymerization, modifier, and monomer stability.

Moreover, taking into account the mentioned factors, the steady-state topological zone will be wider than during the direct electropolymerization, as there are fewer factors capable of destabilizing the steady-state [33–35]. Depending in the monomer concentration and on the electrode shape, the system may be diffusion and reaction-controlled.

Monotonic instability is manifested by an N-shaped part of the voltammogram. It is also caused by DEL influences on the electrochemical reaction. Its condition may be described as:

$$\begin{cases} -\frac{2}{\delta}(\kappa_1 + \mathcal{E}) - \frac{1}{G}(\Lambda + \Omega) < 0 \\ \kappa_1\Omega = -\kappa_1\Lambda - \mathcal{E}\Lambda \end{cases} \quad (11)$$

It may be satisfied only with negative values of Λ and separates the steady, stable states from unstable states.

In the case of polymerization in the presence of complex-forming ions, the complex formation may dissolve the trivalent cobalt in a complex, so these processes may concur. This case will be aborded in our next works.

If the polymerization potential of the monomer is relatively high (as in the case of thiophene), the $\text{CoO}(\text{OH})/\text{CoO}_2$ may be used. Two scenarios are possible for this case – with and without the chemically induced polymer overoxidation. In the simplest case, the present model may be applied (with some rectification). For the second case, the trivariate mathematical model describing it will be described in our next works.

4. Conclusions

From the theoretical description of the anodic conducting polymer assisted electrodeposition catalyzed by $\text{CoO}(\text{OH})$, it is possible to conclude that from the electrosynthetical point of view, this process has to be more efficient than the direct electropolymerization due to the better probability of stable steady-state. The oscillatory instability, in this case, is possible, but it is less probable than in the case of direct electropolymerization, being caused uniquely by electrochemical factors. Depending on the monomer concentration and electrode shape, the electrosynthesis may be diffusion and kinetically controlled.

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Conflicts of Interest

The authors declare no conflict of interest.

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